

A real world application of secure multi-party computations

Duplicate bridge for cheapskates

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The 16th International Workshop on Security Protocols

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Flaws and corrections

Case study

Error detection/correction

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1st permutation

Order the suits: Clubs Hearts Spades Diamonds

1143 2323 4422 1143 2411 4143

1332 4344 1223 2433 1211 3242

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2nd permutation

3231 1224 1243 4421 1233 4421

1311 1432 3332 2441 2244 3332

4141

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	♠ 82	
	♥ A3	
	♦ AQ985	
	♣ Q854	
♠ KT95		♠ A43
♥ KJ9		♥ T86
♦ 432		♦ J76
♣ KJ6		♣ 9732
	♠ QJ76	
	♥ Q7542	
	♦ KT	
	♣ AT	

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Multi-party protocols

Traditionally

- ▶ Secret inputs to each party generating a shared result
- ▶ Computations done on computer

For duplimating

- ▶ Secret result, known inputs
- ▶ 'Computations' done by humans
- ▶ Intermediate state can be secret

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Attacker model

- ▶ Assume the players are inherently trustworthy
 - ▶ They can cheat anyway if not
 - ▶ Most players are trustworthy
- ▶ Players are sufficiently intelligent to make use of small amounts of information
- ▶ Main security goals:
 - ▶ Ensure neither dealer can deduce much about the hands while dealing...
 - ▶ ...and having seen one of the hands.

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1. Generate random P_T ; $T = \{S\}_{E_{P_T}}$
2. Discard P_T
3. Generate random P_1 and P_I
4. Calculate P_2 s.t. $T = \{\{S_{P_I}\}_{E_{P_1}}\}_{E_{P_2}}$
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Suit of the first card dealt

- ▶ Last thirteen cards in P_1 same suit.
- ▶ Likely that there will be a 1 in the last 13 numbers of P_1 .
- ▶ Implies first card of P_2 is that suit.
- ▶ First hand dealt in P_2 does not have a void in that suit.

Solution

Randomize the order of the suits in P_1 .

But...

Hands must be shuffled before going into the boards, else the second dealer can infer the suit order from the order of the cards in their hands.

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Locating high cards

- ▶ High cards from first suit will be at the bottom of some of the piles
- ▶ One of positions $\{13, 26, 39, 52\}$ in P_2 will hold an ace.

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Randomize the number of cards in each pile at the end of P_1 .

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- ▶ Two trials, 3 sessions in November–December 2007, 6 sessions in January–March 2008.
- ▶ Approximately six dealers in total, three pairs.
- ▶ Time to deal 28 boards consistently 10–15 minutes.
- ▶ Observed error rate 4–6 boards, with one perfect result.

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- ▶ Ignore errors.

Detection only

- ▶ Check at some point during the play against the hand record for that board.

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Trial error results

Session	Failures	Recoverable Errors
14/03/08	1	3
07/03/08	2	3
22/02/08	0	0
15/02/08	2	2
07/02/08	3	4
31/02/08	4	2
30/11/07	5	2
16/11/07	7	1
01/11/07	4	1

Table: Errors in each session